## 4-2 Additional Practice <br> Graphing Rational Functions

Use long division to rewrite each rational function. Sketch the graph and identify the asymptotes.

1. $f(x)=\frac{2 x}{x+1}$

2. $f(x)=\frac{2 x^{2}}{x^{2}-1}$


Identify the vertical and horizontal asymptotes of each rational function.
3. $f(x)=\frac{2 x^{2}}{4 x^{2}-1}$
4. $f(x)=\frac{2 x^{2}+10 x+12}{x^{2}-9}$

Graph each function. Label all the horizontal and vertical asymptotes.
5. $f(x)=\frac{10 x+20}{10 x^{2}-49 x-33}$

6. $f(x)=\frac{x^{2}-4 x-6}{2 x^{2}-10 x-12}$

7. You start a business typing papers for students and spend $\$ 3,500$ on a computer and office furniture. You estimate additional costs at $\$ 0.02$ per page. Write a rational function to model the total average cost per page for the first year.
8. The graph of a rational function has vertical asymptotes at $x=-3$ and $x=3$ and a horizontal asymptote at $y=1$. Write a function that has those attributes. Then graph the function to verify that it is correct.


